

Directions: Verify each trigonometric identity. Complete all work on a separate piece of paper.

- 1) $\cos^3 \theta + \sin^2 \theta \cos \theta = \cos \theta$
- 2) $\csc^2 \theta - \cos^2 \theta \csc^2 \theta = 1$
- 3) $\sec \theta \sin \theta = \tan \theta$
- 4) $\frac{\csc \theta}{\sec \theta} = \cot \theta$
- 5) $\frac{\sec^2 \theta - 1}{\tan \theta} = \tan \theta$
- 6) $\frac{\cot \theta}{\csc^2 \theta - 1} = \tan \theta$
- 7) $\sec \theta \sin \theta \cot \theta = 1$
- 8) $\cot \theta \csc \theta \tan^2 \theta = \sec \theta$
- 9) $\cos^2 \theta - \sin^2 \theta = 2 \cos^2 \theta - 1$
- 10) $\cos^2 \theta - \sin^2 \theta = 1 - 2 \sin^2 \theta$
- 11) $\cot \theta \sin \theta = \cos \theta$
- 12) $\frac{\tan \theta}{\sec \theta} = \sin \theta$
- 13) $\sin \theta (1 + \csc \theta) = \sin \theta + 1$
- 14) $(1 + \tan \theta)^2 = \sec^2 \theta + 2 \tan \theta$
- 15) $(1 + \tan^2 \theta) \cos^2 \theta = 1$
- 16) $\cos \theta = \sec \theta - \sin \theta \tan \theta$
- 17) $(\sec \theta + \tan \theta)(\sec \theta - \tan \theta) = 1$
- 18) $\frac{\sec \theta}{\csc^2 \theta} = \sec \theta - \cos \theta$
- 19) $\frac{1 - 2 \csc \theta}{\cot \theta} = \tan \theta - 2 \sec \theta$
- 20) $\frac{\sec^2 \theta - 1}{\tan \theta} = \tan \theta$
- 21) $\sin \theta + \cos \theta \cot \theta = \csc \theta$
- 22) $\cos \theta (\csc \theta - \sec \theta) = \cot \theta - 1$
- 23) $\frac{\cos \theta}{1 - \sin^2 \theta} = \sec \theta$
- 24) $\tan^2 \theta - \tan^2 \theta \sin^2 \theta = \sin^2 \theta$
- 25) $\frac{\cot \theta}{1 + \cot^2 \theta} = \sin \theta \cos \theta$
- 26) $\frac{1 + \tan^2 \theta}{\cos^2 \theta} = \sec^4 \theta$
- 27) $\frac{\sin \theta + \cos \theta}{\sin \theta \cos \theta} = \sec \theta + \csc \theta$
- 28) $\frac{\sec \theta + \tan \theta}{\cos \theta + \cot \theta} = \sin \theta \sec^2 \theta$
- 29) $\frac{(1 + \sin \theta)^2}{\cos^2 \theta} = \frac{1 + \sin \theta}{1 - \sin \theta}$
- 30) $\frac{1 + \sec \theta}{\tan \theta + \sin \theta} = \csc \theta$
- 31) $\csc \theta \cos^2 \theta + \sin \theta = \csc \theta$
- 32) $\frac{\csc^2 \theta}{\csc^2 \theta - 1} = \sec^2 \theta$
- 33) $\sin \theta \left(\frac{\cot \theta}{\sec \theta} + \csc \theta \right) = \cos^2 \theta + 1$
- 34) $\frac{2 \cos^2 \theta - \sin^2 \theta + 1}{\cos \theta} = 3 \cos \theta$
- 35) $\csc \theta - \sin \theta = \cot \theta \cos \theta$
- 36) $\frac{1}{1 - \cos \theta} + \frac{1}{1 + \cos \theta} = 2 \csc^2 \theta$

Extra Practice

$$1) \quad \frac{1+\tan\theta}{\tan\theta} = 1 + \cot\theta$$

$$3) \quad \csc^4\theta - \cot^4\theta = 2 \csc^2\theta - 1$$

$$5) \quad \frac{1+\sec\theta}{\tan\theta+\sin\theta} = \csc\theta$$

$$7) \quad \frac{1}{\sec\theta-\tan\theta} = \sec\theta + \tan\theta$$

$$9) \quad 1 - \sin\theta = \tan\theta (\cot\theta - \cos\theta)$$

$$11) \quad (\sec\theta - \tan\theta)^2 = \frac{1-\sin\theta}{1+\sin\theta}$$

$$13) \quad \sqrt{\frac{\sec\theta+\tan\theta}{\sec\theta-\tan\theta}} = \frac{1+\sin\theta}{\cos\theta}$$

$$15) \quad \sin^2\theta \left(\frac{\csc^2\theta-1}{\cos^2\theta} - \cot^2\theta \right) = \sin^2\theta$$

$$16) \quad (\sin\theta - \cos\theta)^2 + 2\sin\theta - \cos\theta = (1 + 2\sin\theta)(1 - \cos\theta)$$

$$2) \quad \frac{\cos\theta+\tan\theta}{\sin\theta} = \sec\theta + \cot\theta$$

$$4) \quad \frac{\cos\theta+\cot\theta}{\csc\theta+1} = \cos\theta$$

$$6) \quad \frac{2-\sec^2\theta}{\sec\theta} = \frac{1-2\sin^2\theta}{\cos\theta}$$

$$8) \quad 1 + \cos\theta = \cot\theta (\sin\theta + \tan\theta)$$

$$10) \quad \frac{\tan\theta}{1+\tan^2\theta} = \sin\theta \cos\theta$$

$$12) \quad \sqrt{\frac{1-\cos\theta}{1+\cos\theta}} = \frac{1-\cos\theta}{\sin\theta}$$

$$14) \quad \sin^4\theta - \cos^4\theta = 1 - 2\cos^2\theta$$